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Water Transport in Brain:

Cerebrospinal Fluid, Capillaries and Glial Cells



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Cerebrospinal Fluid (CSF)





- Buoyancy
 - Reduce the net weight from 1400 g to 25 g
- Epidural

Subdural haemorrhage

- Protection
 - Prevent contact between delicate neural structures and the surrounding bones
 - Protect from injuries, EX: Jolt, hit
- Transport
 - Nutrients, Chemical messengers, and Metabolic waste products



http://blog.iilm.edu/2012/11/the -rest-is-history/footer_newton/



http://egoscueportland.wordpress.com/2010/12/26/the-cause-and-effect-of-football-tackling/



http://www.expertboxing.com/boxing-strategy/counterpunching/7-easy-boxing-counters-punches





Water Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells

Cerebrospinal Fluid (CSF)

- The choroid plexus produces CSF at a rate of around 500 ml/day
- The total volume of CSF at any given moment is around 150 ml
- Entire volume of CSF is replaced approximately every 8 hours
- CSF circulation path









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Cerebrospinal Fluid (CSF) - Circulation



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Choroid Plexus (CP)



- There are four choroid plexi in each ventricles.
- The CP acts as a blood-CSF barrier (filtration system).
- The CP plays an important role to maintain the delicate extracellular environment



(M. McKinley and V. D. O'Loughlin, Human Anatomy 3rd)

Water Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells





Capillaries

- Around 5-10 µm in diameter
- Smallest blood vessels in brain
- Connect arterioles and venulae
- Site of mass transfer between blood and surrounding tissue, such as oxygen, carbon dioxide, water, ions and so on
- The regulation of behaviour via water channel, AQP4, is one of important issues that we are considering in this research



Costantino Iadecola & Maiken Nedergaard Nature Neuroscience **10**, 1369 - 1376 (2007)





Water Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells

Glial Cells (Neuroglia)

Central Nervous System (CNS)

- Astrocytes
 - Maintain Blood-Brain Barrier
 - Provide structural framework
 - Regulate ions and nutrients
 - Absorb and recycle neurotransmitters
- Oligodendrocytes
 - Mylinate CNS axons
 - Provide structural framework
- Microglia Cells
 - Remove cell debris, waste products, pathogens by phagocytosis
- Ependymal Cells
 Assist for producing and circulating CSF

Peripheral Nervous System (PNS)

- Satellite Cells
- Schwann Cells









(M. McKinley and V. D. O'Loughlin, Human Anatomy 3rd)

Water Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells





- Discovery aquaporin Peter Agre
 - the biochemical properties of the Rh proteins from the erythrocyte membrane
 - Reveal the homology with MIP by cloning the full-length cDNA sequence



• The structure of aquaporin

(http://www.hopkinsmedicine.org/press/2003/october/031008a.htm)



(PubMed:18678926, 2008)



(Suzuki H, Nishikawa K, Hiroaki Y, Fujiyoshi Y., 2008)



(TCB Group, UIUC)





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⁽H. Lodish, Molecualr Cell Biology 7th, 2012)

- Effects of AQPs
 - Expression of water permeability of AQP 1 in Xenopus laevis oocytes
 - The upper oocytes were injected with mRNA encoding AQP in each photo transfer from an isotonic salt solution to a hypotonic salt solution
 - The lower oocytes in each photo are normally not permeable to water (without AQP 1 expression)
 - From 2.5 min to 3.5 min, the lower oocytes continue to keep their original shape because of impermeability. However, the upper oocytes continue to swell due to osmotic water flux-in. This phenomenon implies that AQP is a water channel protein (WCP)





Phylogenetic tree of Aquaporins







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Multiscale Platform







Water Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells

Multiple-Network Poroelastic Theory (MPET) Model

- The concept of MPET comes from geotechnical engineering in order to describe fluid transport phenomena in soil and rock
- It is assembled by deformable elastic matrix and multiple fluid networks of pores and fissures
- This porous media model vary with porosity and permeability
- Equations are built by treating the different fluid networks as separate compartments which are in communication each other







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- The concept of MPET model can capture the dynamics of all fluids transfer in the brain
- Extend to include independent networks for cerebral blood and CSF
- Distinguish four network compartments
 - 1. Arterial blood
 - 2. Arteriole/Capillary blood
 - 3. Cerebrospinal fluid
 - 4. Venous blood







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- Two governing equations of motion for a unit volume
 - a. Solid-fluid equation of motion

$$\nabla \cdot \sigma^{M} + \rho_{f} \left(f^{b} - \frac{\partial^{2} x}{\partial t^{2}} \right) - \sum_{a=1}^{A} \alpha^{a} \nabla p^{a} = 0$$

b. Fluid equilibrium and conservation (each network A = 1,...,a)

$$\frac{1}{Q^{a}}\frac{\partial p}{\partial t} + \alpha^{a}\frac{\partial \left(\nabla \bullet x\right)}{\partial t} - \sum_{b=1, b\neq a}^{A} \dot{S}_{b\rightarrow a} + \nabla \bullet \left[\kappa^{a} \bullet \rho_{f}^{a}\left(f^{b} - \frac{\partial^{2} x}{\partial t^{2}}\right) - \kappa^{a} \bullet \nabla p^{a}\right] = 0$$

Setting A=4 from previous slide and assuming a linear stressstrain relationship, we have following *u-p* formulations





 Linear stress strain equation (Hooke's law) inverted for stress and then stress is represented as a function of displacement and where the permeability is isotropic

$$\nabla \cdot \boldsymbol{\sigma}^{M} = G \nabla^{2} \boldsymbol{x} + \frac{G}{1 - 2\nu} \nabla (\nabla \cdot \boldsymbol{x}) \quad \nabla \cdot \boldsymbol{\sigma}^{M} + \rho_{f} \left(\boldsymbol{f}^{b} - \ddot{\boldsymbol{x}} \right) - \alpha^{a} \nabla p^{a} - \alpha^{e} \nabla p^{e} - \alpha^{c} \nabla p^{c} - \alpha^{\nu} \nabla p^{\nu} = 0$$

$$\frac{1}{Q^{a}}\frac{\partial p^{a}}{\partial t} + \alpha^{a}\frac{\partial(\nabla \cdot \mathbf{x})}{\partial t} - \dot{S}_{c \to a} - \dot{S}_{e \to a} - \dot{S}_{v \to a} + \nabla \cdot \left[\kappa^{a} \cdot \rho_{f}^{a}\left(f^{b} - \ddot{\mathbf{x}}\right) - \kappa^{a} \cdot \nabla p^{a}\right] = 0$$

$$\frac{1}{Q^{e}}\frac{\partial p^{e}}{\partial t} + \alpha^{e}\frac{\partial(\nabla \cdot \mathbf{x})}{\partial t} - \dot{S}_{a \to e} - \dot{S}_{c \to e} - \dot{S}_{v \to e} + \nabla \cdot \left[\kappa^{e} \cdot \rho_{f}^{e}\left(f^{b} - \ddot{\mathbf{x}}\right) - \kappa^{e} \cdot \nabla p^{e}\right] = 0$$

$$\frac{1}{Q^{e}}\frac{\partial p^{c}}{\partial t} + \alpha^{c}\frac{\partial(\nabla \cdot \mathbf{x})}{\partial t} - \dot{S}_{a \to c} - \dot{S}_{v \to c} + \nabla \cdot \left[\kappa^{c} \cdot \rho_{f}^{c}\left(f^{b} - \ddot{\mathbf{x}}\right) - \kappa^{c} \cdot \nabla p^{c}\right] = 0$$

$$\frac{1}{Q^{v}}\frac{\partial p^{v}}{\partial t} + \alpha^{v}\frac{\partial(\nabla \cdot \mathbf{x})}{\partial t} - \dot{S}_{a \to v} - \dot{S}_{e \to v} - \dot{S}_{c \to v} + \nabla \cdot \left[\kappa^{v} \cdot \rho_{f}^{v}\left(f^{b} - \ddot{\mathbf{x}}\right) - \kappa^{v} \cdot \nabla p^{v}\right] = 0$$





Nater Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells



• The one-dimensional spherically symmetric system equations:

$$\begin{aligned} \frac{\partial^{2}x}{\partial r^{2}} + \frac{2}{r}\frac{\partial x}{\partial r} - \frac{2}{r^{2}}x &= \frac{1-2\nu}{2G(1-\nu)} \left[\alpha^{a}\frac{\partial p^{a}}{\partial r} + \alpha^{e}\frac{\partial p^{e}}{\partial r} + \alpha^{c}\frac{\partial p^{c}}{\partial r} + \alpha^{v}\frac{\partial p^{v}}{\partial r} - \rho_{f}\left(f_{r}^{b} - \ddot{x}\right) \right] \\ \frac{1}{Q^{a}}\frac{\partial p^{a}}{\partial t} + \alpha^{a}\frac{\partial}{\partial t}\left(\frac{\partial x}{\partial r} + \frac{2}{r}x\right) - \dot{S}_{c \to a} - \dot{S}_{e \to a} - \dot{S}_{v \to a} + \frac{2}{r}\rho_{f}^{a}\left(f_{r}^{b} - \ddot{x}\right) - \kappa^{a}\left(\frac{\partial^{2}p^{2}}{\partial r^{2}} + \frac{2}{r}\frac{\partial p^{a}}{\partial r}\right) + \kappa^{a}\left(\frac{\partial \rho_{f}^{a}\left(f_{r}^{b} - \ddot{x}\right)}{\partial r}\right) = 0 \\ \frac{1}{Q^{e}}\frac{\partial p^{e}}{\partial t} + \alpha^{e}\frac{\partial}{\partial t}\left(\frac{\partial x}{\partial r} + \frac{2}{r}x\right) - \dot{S}_{a \to e} - \dot{S}_{c \to e} - \dot{S}_{v \to e} + \frac{2}{r}\rho_{f}^{e}\left(f_{r}^{b} - \ddot{x}\right) - \kappa^{e}\left(\frac{\partial^{2}p^{2}}{\partial r^{2}} + \frac{2}{r}\frac{\partial p^{e}}{\partial r}\right) + \kappa^{e}\left(\frac{\partial \rho_{f}^{e}\left(f_{r}^{b} - \ddot{x}\right)}{\partial r}\right) = 0 \\ \frac{1}{Q^{e}}\frac{\partial p^{e}}{\partial t} + \alpha^{e}\frac{\partial}{\partial t}\left(\frac{\partial x}{\partial r} + \frac{2}{r}x\right) - \dot{S}_{a \to e} - \dot{S}_{e \to e} - \dot{S}_{v \to e} + \frac{2}{r}\rho_{f}^{e}\left(f_{r}^{b} - \ddot{x}\right) - \kappa^{e}\left(\frac{\partial^{2}p^{2}}{\partial r^{2}} + \frac{2}{r}\frac{\partial p^{e}}{\partial r}\right) + \kappa^{e}\left(\frac{\partial \rho_{f}^{e}\left(f_{r}^{b} - \ddot{x}\right)}{\partial r}\right) = 0 \\ \frac{1}{Q^{e}}\frac{\partial p^{v}}{\partial t} + \alpha^{e}\frac{\partial}{\partial t}\left(\frac{\partial x}{\partial r} + \frac{2}{r}x\right) - \dot{S}_{a \to a} - \dot{S}_{e \to c} - \dot{S}_{v \to c} + \frac{2}{r}\rho_{f}^{e}\left(f_{r}^{b} - \ddot{x}\right) - \kappa^{e}\left(\frac{\partial^{2}p^{2}}{\partial r^{2}} + \frac{2}{r}\frac{\partial p^{e}}{\partial r}\right) + \kappa^{e}\left(\frac{\partial \rho_{f}^{e}\left(f_{r}^{b} - \ddot{x}\right)}{\partial r}\right) = 0 \\ \frac{1}{Q^{v}}\frac{\partial p^{v}}{\partial t} + \alpha^{v}\frac{\partial}{\partial t}\left(\frac{\partial x}{\partial r} + \frac{2}{r}x\right) - \dot{S}_{a \to v} - \dot{S}_{e \to v} - \kappa^{v}\left(\frac{\partial^{2}p^{2}}{\partial r^{2}} + \frac{2}{r}\frac{\partial p^{v}}{\partial r}\right) + \kappa^{v}\left(\frac{\partial \rho_{f}^{v}\left(f_{r}^{b} - \ddot{x}\right)}{\partial r}\right) = 0 \\ \frac{1}{Q^{v}}\frac{\partial p^{v}}{\partial t} + \alpha^{v}\frac{\partial}{\partial t}\left(\frac{\partial x}{\partial r} + \frac{2}{r}x\right) - \dot{S}_{a \to v} - \dot{S}_{e \to v} - \dot{S}_{e$$





Nater Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells

Biological MPET Model Assumptions

- Spherically symmetric geometry
- No external forces on the system
- Gravity is neglected
- Use a stationary reference frame
- Long time scale for development of hydrocephalus so the system is assumed as quasi-steady
- Transfer of fluid between networks does not break laws of continuity for the system, hence directional transport is important ($|\dot{S}|$ >0 is a loss from the system)



Tully, B. and Y. Ventikos, *Cerebral water transport using multiplenetwork poroelastic theory: application to normal pressure hydrocephalus.* Journal of Fluid Mechanics, 2011

Water Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells





- Darcy Flow
 - $Q = -\frac{\kappa}{\mu} \cdot A \cdot \Delta p$
- The Starling's Law of filtration equation
 - $J_{v} = L_{p}\tilde{S}\left(\Delta p \Delta\Pi\right)$
- Permeability coefficient (Isotropic)

$$\kappa_{AQP} = \left(\frac{\kappa_{e}}{\mu_{e}}\right) \left[1 - \left(\frac{p_{e} - p_{ref}}{p_{ref}}\right)\right] A_{f}$$



Water Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells





Darcy Flow

$$Q = -\frac{\kappa}{\mu} \cdot A \cdot \Delta p$$

• The Starling's Law of filtration equation

$$J_{v} = L_{p}\tilde{S}\left(\Delta p - \Delta\Pi\right)$$

Permeability coefficient (Isotropic)

$$\kappa_{AQP} = \left(\frac{\kappa_{e}}{\mu_{e}}\right) \left[1 - \left(\frac{p_{e} - p_{ref}}{p_{ref}}\right)\right] A_{f}$$







Water Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells

Darcy Flow

$$Q = -\frac{\kappa}{\mu} \cdot A \cdot \Delta p$$

• The Starling's Law of filtration equation

$$J_{v} = L_{p}\tilde{S}\left(\Delta p - \Delta\Pi\right)$$

Permeability coefficient (Isotropic)

$$\kappa_{AQP} = \left(\frac{\kappa_{e}}{\mu_{e}}\right) \left[1 - \left(\frac{p_{e} - p_{ref}}{p_{ref}}\right)\right] A_{f}$$







Water Transport in Brain: Cerebrospinal Fluid, Capillaries and Glial Cells

- Darcy Flow
- $Q = -\frac{\kappa}{\mu} \cdot A \cdot \Delta p$ The Starling's Law of filtration equation $J_{\nu} = L_{p}\tilde{S} \left(\Delta p - \Delta \Pi\right)$
- Permeability coefficient (Isotropic)

$$\kappa_{AQP} = \left(\frac{\kappa_e}{\mu_e}\right) \left[1 - \left(\frac{p_e - p_{ref}}{p_{ref}}\right)\right] A_f$$



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MPET Model – Currently Progress

 After the assumptions discussed, the MPET governing equations can be cast as following:

$$\frac{\partial^{2} x}{\partial r^{2}} + \frac{2}{r} \frac{\partial x}{\partial r} - \frac{2}{r^{2}} x = \frac{1 - 2\nu}{2G(1 - \nu)} \left[\alpha^{a} \frac{\partial p^{a}}{\partial r} + \alpha^{e} \frac{\partial p^{e}}{\partial r} + \alpha^{c} \frac{\partial p^{c}}{\partial r} + \alpha^{v} \frac{\partial p^{v}}{\partial r} - \rho_{f} \left(f_{r}^{b} - \ddot{x} \right) \right]$$

$$\kappa_{AQP} = \left(\frac{\kappa_{e}}{\mu_{e}} \right) \left[1 - \left(\frac{p_{e} - p_{ref}}{p_{ref}} \right) \right] A_{f} - \kappa^{a} \left(\frac{\partial^{2} p^{a}}{\partial r^{2}} + \frac{2}{r} \frac{\partial p^{a}}{\partial r} \right) + \left| \dot{s}_{a \to c} \right| = 0 \qquad J_{\nu} = L_{p} \tilde{S} \left(\Delta p - \Delta \Pi \right)$$

$$-\kappa^{e} \left(\frac{\partial^{2} p^{e}}{\partial r^{2}} + \frac{2}{r} \frac{\partial p^{e}}{\partial r} \right) - \left| \dot{s}_{c \to e} \right| + \left| \dot{s}_{e \to \nu} \right| = 0$$

$$-\kappa^{c} \left(\frac{\partial^{2} p^{c}}{\partial r^{2}} + \frac{2}{r} \frac{\partial p^{v}}{\partial r} \right) - \left| \dot{s}_{a \to c} \right| + \left| \dot{s}_{c \to v} \right| = 0$$

$$-\kappa^{v} \left(\frac{\partial^{2} p^{v}}{\partial r^{2}} + \frac{2}{r} \frac{\partial p^{v}}{\partial r} \right) - \left| \dot{s}_{e \to v} \right| - \left| \dot{s}_{c \to v} \right| = 0$$





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MPET Model Processes





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Biological MPET Model – What we would like to do?

- Assist to explore numerous cerebral pathologies
 - brain oedema
 - brain trauma
 - brain tumors
 - stroke,
 - Hydrocephalus
 - Migraines
 - other neurological pathologies, such as multiple sclerosis (MS) and neuromyelitis optica (NMO)
- Aims to make a tangible contribution to the understanding of cerebral or neurological pathologies, but also to pharmaceuticals development.





Hydrocephalus (HCP)

- HCP can be described as the abnormal accumulation of CSF with in the brain.
- Types of HCP:
 - a. Obstructive HCP
 - b. Communicating HCP
 - c. Normal Pressure Hydrocephalus (NPH)
 - Symptoms in adults:
 - a. Headache
 - b. Vomiting
 - c. Altered level of consciousness
 - d. Visual obscurations
 - e. Cognitive impairment, poor concentration, gait disturbance



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Hydrocephalus (HCP)

Treatment	Location of Fluid Drain
Ventriculo-peritoneal shunt (VP shunt)	Peritoneal cavity
Ventriculo-atrial shunt (VA shunt)	Right atrium of the heart
Ventriculo-pleural shunt (VPL shunt)	Pleural cavity
Endoscopic third ventriculostomy (ETV) Choroid plexus cauterization (CPC)	The floor of the 3 rd ventricle Choroid plexus cauterization



VA SHUNT



















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Comparing the effect of AQP presence on the ventricular displacement in a case involving an open cerebral aqueduct Comparing different amplification factors for the ventricular displacement in transient development



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Comparing the effect of AQP presence on the ventricular pressure in a case involving an open/severe cerebral aqueduct

Comparing the effect of AQP presence on the ventricular displacement in a case involving an open/severe cerebral aqueduct



FBG

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Velocity distribution in open cerebral aqueduct with AQP effect

Velocity distribution in open cerebral aqueduct without AQP effect







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Current Results : Choroid Plexus + ETV



- The severe case causes a ventricular displacement of just over 3.3 mm, mild (0.55mm), open case (0.5 mm)
- ETV significantly reduces displacement of mild stenosis to the open level



- CSF pressure is lowest in severely stenosed case (966 Pa)
- Open and mild cases exhibit similar pressure distributions (1070-1072 Pa). All converge to 1089 Pa at skull
- ETV reduces the pressure in both mild and severe cases





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- (Left) Sagittal view of a z-slic of the unobstructed ventricular system
- (Centre) Rotated view of lines tangent to the instantaneous velocity vector in the AS and 4th ventricle (open case)
- (Right) Sagittal view of lines tangent to the instantaneous velocity vector in the 3rd ventricle and both LV's





Impact & Applications

- Scientific impact
 - a. To develop a completely new understanding of brain water balance
 - b. Virtual Physiological Brain (VP-Brain) is its target of the development of virtual optical instrumentation
- Clinical impact
 - a. To improve diagnosis, intervention planning and therapy design
 - b. To facilitate targeted clinical interventions, which reduces the risk of ineffective, or harmful, treatment, and improves patient safety and clinical outcomes
- Industrial impact
 - a. Three targeted industrial applications
 - 1. Accurate characterisation of brain injury by modelling head impact
 - 2. Development and deployment of a novel combined ICP-NIRS probe
 - 3. Design of novel shunting devices
 - b. The pharmaceutical industry can realise new product development





Thanks !!



Questions, please!!

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- ESI-Group







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