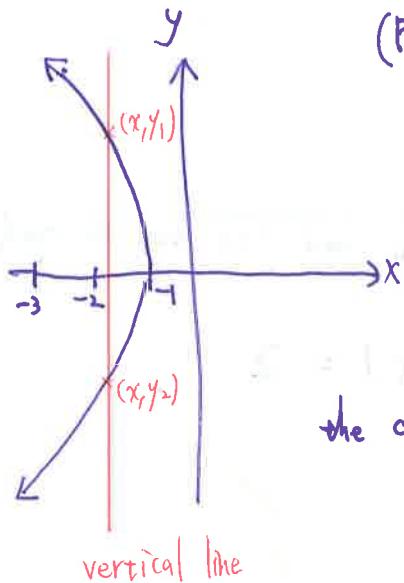


1.5 #46.

State whether the curve is the graph of a function.

If it is, give the domain and the range.



(P.26) A curve C which intersects each vertical line at most once is the graph of a function.

the curve is not the graph of a function.

1.5 #30.

Form the composition $f \circ g$ and give the domain.

$$f(x) = \sqrt{1-x}, \quad x \leq 1$$

(P.43)

$$(f \circ g)(x) = f(g(x))$$

$$g(x) = 2\cos x, \quad 0 \leq x \leq 2\pi$$

$$\text{dom}(f \circ g) = \left\{ x \in \text{dom}(g) \mid g(x) \in \text{dom}(f) \right\}$$

(1)

$$(f \circ g)(x) = f(g(x)) = f(2\cos x) = \sqrt{1 - 2\cos x}, \quad \text{dom}(f \circ g) = \left[\frac{\pi}{3}, \frac{5\pi}{3} \right]$$

since $g(x) \in \text{dom}(f) \Rightarrow 2\cos x \leq 1 \Rightarrow \cos x \leq \frac{1}{2}$ and $0 \leq x \leq 2\pi$ ($x \in \text{dom}(g)$)

$$\Rightarrow \frac{\pi}{3} \leq x \leq \frac{5\pi}{3}$$

(2)

$$(g \circ f)(x) = g(f(x)) = g(\sqrt{1-x}) = 2\cos(\sqrt{1-x}), \quad \text{dom}(g \circ f) = [-4\pi^2 + 1, 1]$$

$$\text{dom}(g \circ f) = \left\{ x \in \text{dom}(f) \mid f(x) \in \text{dom}(g) \right\}$$

since $f(x) \in \text{dom}(g) \Rightarrow 0 \leq \sqrt{1-x} \leq 2\pi \Rightarrow 0 \leq 1-x \leq 4\pi^2 \Rightarrow -4\pi^2 + 1 \leq x \leq 1$

and $x \leq 1$ ($x \in \text{dom}(f)$) $\Rightarrow -4\pi^2 + 1 \leq x \leq 1$

2.1 #42

Decide on intuitive grounds whether or not the indicated limit exists; evaluate the limit if it does exist.

$$f(x) = \begin{cases} 2x & , x < 1 \\ x^2 + 1 & , x \geq 1 \end{cases} \quad \lim_{x \rightarrow 1} f(x) = \underline{\underline{2}}$$

(P59.) For a full limit to exist, both one-side limits have to exist and they have to equal.

$$\lim_{x \rightarrow 1^+} f(x) = \lim_{x \rightarrow 1^+} (x^2 + 1) = 2 \quad \lim_{x \rightarrow 1^-} f(x) = \lim_{x \rightarrow 1^-} (2x) = 2$$

$$\lim_{x \rightarrow 1} f(x) = \lim_{x \rightarrow 1^+} f(x) = \lim_{x \rightarrow 1^-} f(x) = 2$$

2.3 #16. Evaluate the limits that exist. $\lim_{h \rightarrow 0} h(1 - \frac{1}{h}) = \underline{\underline{-1}}$

$$\lim_{h \rightarrow 0} h(1 - \frac{1}{h}) = \lim_{h \rightarrow 0} (h - 1)$$

$$= 0 - 1$$

$$= -1$$