Name and Student ID's: $\qquad$

## Homework 11, Advanced Calculus 2

1. Prove that the Implicit Function Theorem implies the Inverse Function Theorem.
2. Prove that the Rank Theorem implies the Inverse Function Theorem.
3. Let $F: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}$ be define by

$$
F(x, y)=\left(e^{x} \cos y, e^{x} \sin y\right) .
$$

(a) What is the range of $F$ ?
(b) Prove that $D F$ is invertible everywhere. However, $F$ is not a bijective map.
4. Bartle Section 41: E, G, J, M, O.
5. Bartle Section 42: D, K, M, W.

