Numerical Differential Equations Homework 2

(Due: May. 17, 2007)

1. Problem 1

Chapter 2, page 37, Exercise 2.2

2. Problem 2

Chapter 2, page 37, Exercise 2.3

3. Problem 3

Use (2.10) to write a program to solve the boundary value problem:

$$u''(x) = f(x)$$
 for $-1 < x < 1$ (1)

$$u(-1) = \alpha, \qquad u(1) = \beta. \tag{2}$$

Solve the problem with various grid sizes and the conditions below

- $f(x) = 2, \alpha = \beta = 1$
- $f(x) = 12x^2, \ \alpha = \beta = 1$
- $f(x) = e^x$, $\alpha = e^{-1}$, $\beta = e^1$

Discuss the results.